

The Power Rule

The power rule is generally used to differentiate expressions that are raised to any power. It's a shortcut to determine the derivative of a power function.

Formula:

$$\frac{d}{dx}(x^n) = n \cdot x^{n-1}$$

(Basically, take the exponent, multiply it by the coefficient, and decrease the exponent by 1.)

Note:

- n must be a number, not a variable
- x must be a variable, not a number

Examples:

$$\begin{aligned} 1.) \quad y &= x^2 \\ y' &= 2x^1 \end{aligned}$$

$$\begin{aligned} 2.) \quad y &= x^3 + 1 \\ y' &= 3x^2 + 0 \end{aligned}$$

$$\begin{aligned} 3.) \quad f(x) &= x^6 + 2x^5 - 7x^4 + 10 \\ f'(x) &= 6x^5 + 10x^4 - 28x^3 \end{aligned}$$

$$\begin{aligned} 4.) \quad f(x) &= \frac{1}{x} \\ f(x) &= x^{-1} \\ f'(x) &= -x^{-2} \end{aligned}$$